# From Al to Computational Social Choice 

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IJCAI-22
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## Social choice theory

Designing and analysing methods for collective decision making


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The poll is opened until March 25, 2025 (unless the poll creator decides to close it before).

## Social choice theory

Designing and analysing methods for collective decision making


## A very rough history of social choice

1. around 1789: Condorcet and Borda (IJCAI-1789, Bastille)
2. 1951: birth of social choice theory (economics/mathematics); mostly axiomatic results such as impossibility theorems (most celebrated: Arrow's)
3. from the 1990's: computational turn.

Edith Elkind's IJCAI-21 talk:
https://ijcai-21.org/videos-slides/?video=InvT1

## Social Choice Rules

- input: agents express preferences over alternatives/candidates
- output: an alternative

Choose the temperature in the room? Various input formats

| Ann: | 17 | Ann: | $17 \succ 18 \succ 19 \succ 20$ |
| :--- | :--- | :--- | :--- |
| Bob: | 20 | Bob: | $20 \succ 19 \succ 18 \succ 17$ |
| Carol: | 19 | Carol: | $19 \succ 20 \succ 18 \succ 17$ |
| David: | 17 | David: | $17 \succ 18 \succ 19 \succ 20$ |
| uninominal |  | ordinal |  |


|  | 17 | 18 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: |
| Ann | + | + | + |  |
| Bob |  |  |  | + |
| Carol |  | + | + | + |
| David | + | + |  |  |
| approvals |  |  |  |  |


|  | 17 | 18 | 19 | 20 |
| :---: | :---: | :---: | :---: | :---: |
| Ann | 50 | 30 | 20 | 0 |
| Bob | 0 | 0 | 0 | 100 |
| Carol | 0 | 40 | 50 | 10 |
| David | 40 | 30 | 20 | 10 |
|  | evaluations |  |  |  |

## Al and Computational Social Choice

AI / CS have contributed to reshape social choice:

- new techniques
- new paradigms
- new objects of study, new applications

This talk: a quick guided tour of computational social choice via a non-exhaustive, biased selection of problems.

WARNING: My slides contain no references.
Key references are on supplementary slides, and also on a text that comes with it.

## 1. Liquid democracy

- Representative democracy: citizens choose their delegates.
- Liquid/fluid democracy: citizens can choose either to vote on an issue, or to delegate to someone else.
- Direct democracy: citizens express their opinion on any issue.


## 1. Liquid democracy

Committee election
Who should be elected at the new steering board?

Do you want to vote yourself or delegate your vote to a trusted peer?

Classical social choice Aggregating preferences

No ground truth

## 1. Liquid democracy

English idioms
You will be given English idioms, and asked to identify their meaning.

Do you want to vote yourself or delegate your vote to a trusted peer?


Landmarks
You wil be shown pictures of landmarks, and asked to say in which country they are.
don't delegate
Do you want to vote yourself or delegate your vote to a trusted peer?

## 1. Liquid democracy

## English idioms

You will be given English idioms, and asked to identify their meaning. Do you want to vote yourself or delegate your vote to a trusted peer?


Delegation graph


Accuracy

Source: Manon Revel

## 1. Liquid democracy



## Cycles?

Delegations leading nowhere?
abstains
$\rightarrow$ Ranked delegations


Thanks: Manon Revel, Markus Brill, Théo Delemazure, Umberto Grandi

## 2. Epistemic Voting and Crowdsourcing

Epistemic social choice:

- there is a ground truth to be uncovered
- votes are noisy reports
- voting rules are maximum likelihood estimators.
- starts with Condorcet's jury theorem, 1785
$\rightarrow$ Statistical machine learning


## 2. Epistemic Voting and Crowdsourcing



## Crowdsourcing via approval voting

In which of the 20 districts of Paris was this picture taken? You may give several answers. You will get a reward if your selection contains the true answer, minus a penalty that increases with the size of your selection.
2. Epistemic Voting and Crowdsourcing

Crowdsourcing via approval voting

|  | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | expertise? |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ann |  |  |  |  |  |  | + |  |  |  |
| Bob |  |  | + |  | + |  |  | + | + |  |
| Carol |  | + |  | + |  | + |  | + |  |  |
| David |  |  |  |  |  |  | + |  | + |  |
| Eva |  |  | + | + | + | + | + | + | + |  |
| Fred | + |  |  |  |  |  |  |  |  |  |
| Gloria |  |  |  |  | + |  | + | + | + |  |
| $\#$ | 2 | 2 | 2 | 2 | 3 | 2 | 4 | 4 | 4 |  |

2. Epistemic Voting and Crowdsourcing

Crowdsourcing via approval voting

|  | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | expertise? |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ann |  |  |  |  |  |  | + |  |  | high |
| Bob |  |  | + |  | + |  |  | + | + | med- |
| Carol |  | + |  | + |  | + |  | + |  | med- |
| David |  |  |  |  |  |  | $+$ |  | $+$ | med+ |
| Eva |  |  | + | + | + | + | + | $+$ | + | low |
| Fred | + |  |  |  |  |  |  |  |  | low! |
| Gloria |  |  |  |  | + |  | $+$ | $+$ | $+$ | med- |
| \# |  |  |  |  |  |  | $\bullet$ |  |  |  |

Epistemic voting can also be applied to

## 3. Iterated Voting

Plurality voting: the candidate named by the largest number of voters wins.

$$
\begin{array}{ll}
4 \text { voters } & a \succ b \succ c \succ d \succ e \\
3 \text { voters } & e \succ d \succ b \succ c \succ a \\
2 \text { voters } & c \succ e \succ b \succ a \succ d \\
2 \text { voters } & b \succ c \succ d \succ a \succ e
\end{array}
$$

## 3. Iterated Voting

Plurality voting: the candidate named by the largest number of voters wins.

$$
\begin{array}{ll}
4 \text { voters } & a \succ b \succ c \succ d \succ e \\
3 \text { voters } & e \succ d \succ b \succ c \succ a \\
2 \text { voters } & c \succ e \succ b \succ a \succ d \\
2 \text { voters } & b \succ c \succ d \succ a \succ e \\
& \text { winner: } a
\end{array}
$$

## 3. Iterated Voting

Plurality voting: the candidate named by the largest number of voters wins.

4 voters $\quad a \succ b \succ c \succ d \succ e$
3 voters $e \succ d \succ b \succ c \succ a$
2 voters $\quad c \succ e \succ b \succ a \succ d$
2 voters $b \succ c \succ d \succ a \succ e$
previous winner: a
winner: e

## 3. Iterated Voting

Plurality voting: the candidate named by the largest number of voters wins.

$$
\begin{array}{ll}
4 \text { voters } & a \succ b \succ c \succ d \succ e \\
3 \text { voters } & e \succ d \succ b \succ c \succ a \\
2 \text { voters } & c \succ e \succ b \succ a \succ d \\
2 \text { voters } & b \succ c \succ d \succ a \succ e \\
\text { previous winner: } e \\
& \text { winner: } b
\end{array}
$$

Chances are that we have reached convergence.

## 3. Iterated Voting

$$
\begin{array}{lcc}
4 \text { voters } & a \succ b \succ c \succ d \succ e & a \succ b \succ c \succ d \succ e \\
3 \text { voters } & e \succ d \succ b \succ c \succ a & e \succ d \succ b \succ c \succ a \\
2 \text { voters } & c \succ e \succ b \succ a \succ d & c \succ e \succ b \succ a \succ d \\
2 \text { voters } & b \succ c \succ d \succ a \succ e & b \succ c \succ d \succ a \succ e \\
\text { winner } & a & b
\end{array}
$$

- voting rule + voter behaviour model $\rightarrow$ equilibrium reached?
- equilibria sometimes of better quality than sincere outcomes

Thanks: Reshef Meir

## 4. Distortion and low-communication voting

## Metric setting

- alternatives and voters are in a metric space with distance $d$
- cost (or disutility) of alternative $x$ to voter $i: c_{i}(x)=d(i, x)$
- $f$ voting rule with ordinal input?
- distortion of $f$ : worst-case ratio between the cost of the winner according to $f$, and the optimal cost.

- a has a global cost $\sim 3 n / 4 \ldots$ and is the majority winner
- $b$ has a global cost $\sim n / 4$
- when $n=2$, all reasonable voting rules with ordinal input degenerate to majority
- no voting rule with can have distortion smaller than 3 !
- can we find a rule that achieves 3 ?


## 4. Distortion and low-communication voting

Metric setting


## 4. Distortion and low-communication voting

Metric setting


References: supplementary slides + paper!

## 4. Distortion and low-communication voting

Metric setting


References: supplementary slides + paper!

## 4. Distortion and low-communication voting

Metric setting

```
5% Copeland (2015)
    + a very simple rule: IJCAI-2022, Friday 10am
    needs voters to submit only 2 log m bits each
        low-communication voting rule
```

References: supplementary slides + paper!

## 5. Complex alternatives $\rightarrow$ Combinatorial domains

- there are several possible topics I can speak during my talk
- I have time to talk only about two topics
- Ann: would like to hear about $t_{1}$ or $t_{3}$, and about $t_{2}$ or $t_{4}$.
- Bob: likes $t_{1}$ and $t_{4}$, and in case $t_{1}$ is not selected then $t_{2}$.
- Carol: likes $t_{3}$ and that's all.
- focus on preferential dependencies
- use compact preference representation languages, e.g. CP-nets


## 5. Complex alternatives $\rightarrow$ Multiwinner elections

We can now select three topics. The votes of the attendees:


Three possible criteria $\rightarrow$ three families of rules

$$
\begin{array}{ll}
\text { excellence } & t_{1}, t_{2}, t_{3} \\
\text { diversity } & t_{1}, t_{3}, t_{4} \\
\text { proportionality } & t_{1}, t_{2}, t_{5}
\end{array}
$$

## 5. Complex alternatives $\rightarrow$ Multiwinner elections

We can now select three topics. The votes of the attendees:


Three possible criteria $\rightarrow$ three families of rules

$$
\begin{array}{ll}
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\text { proportionality } & t_{1}, t_{2}, t_{5}
\end{array}
$$

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\text { proportionality } & t_{1}, t_{2}, t_{5}
\end{array}
$$

## 5. Complex alternatives $\rightarrow$ Multiwinner elections

We can now select three topics. The votes of the attendees:

|  | $t_{1}$ | $t_{2}$ | $t_{3}$ | $t_{4}$ | $t_{5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{8}$ voters | + | + | + |  |  |
| 3 voters |  |  |  | + |  |
| 1 voter |  |  |  |  | + |

Three possible criteria $\rightarrow$ three families of rules

| excellence | $t_{1}, t_{2}, t_{3}$ |
| :--- | :--- |
| diversity | $t_{1}, t_{3}, t_{4}$ |
| proportionality | $t_{1}, t_{2}, t_{5}$ |

- focus on properties, especially proportionality


## 5. Complex alternatives $\rightarrow$ Participatory budgeting

- topics now have durations
- total budget: 30 minutes



## 5. Complex alternatives $\rightarrow$ Participatory budgeting

- topics now have durations
- total budget: 30 minutes

|  | $t_{1}$ | $t_{2}$ | $t_{3}$ | $t_{4}$ | $t_{5}$ | $t_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $100 \times$ | + | + |  |  |  |  |
| $90 \times$ |  |  | + |  |  |  |
| $30 \times$ |  |  |  | + | + | + |
| $30 \times$ |  |  |  | + | + |  |
| $10 \times$ | + |  |  | + |  |  |
| $\cos t$ | 9 | 9 | 9 | 4 | 4 | 4 |

A more common interpretation:

- $t_{1}, \ldots, t_{6}$ are projects with costs
- total budget: $30 \mathrm{M} €$


## 5. Complex alternatives $\rightarrow$ Participatory budgeting

The greedy method

|  | $t_{1}$ | $t_{2}$ | $t_{3}$ | $t_{4}$ | $t_{5}$ | $t_{6}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $100 \times$ | + | + |  |  |  |  |
| $90 \times$ |  |  | + |  |  |  |
| $30 \times$ |  |  |  | + | + | + |
| $30 \times$ |  |  |  | + | + |  |
| $10 \times$ | + |  |  | + |  |  |
| $\cos t$ | 9 | 9 | 9 | 4 | 4 | 4 |

available budget: 30

| topic | \#votes | cost |  |
| :---: | :---: | :---: | :---: |
| $t_{1}$ | 110 | 9 | $\bullet$ |
| $t_{2}$ | 100 | 9 | $\bullet$ |
| $t_{3}$ | 90 | 9 | $\bullet$ |
| $t_{4}$ | 70 | 4 |  |
| $t_{5}$ | 60 | 4 |  |
| $t_{6}$ | 30 | 4 |  |

Good?

## 5. Complex alternatives $\rightarrow$ Participatory budgeting

|  | $t_{1}$ | $t_{2}$ | $t_{3}$ | $t_{4}$ | $t_{5}$ | $t_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $100 \times$ | + | + |  |  |  |  |
| $90 \times$ |  |  | + |  |  |  |
| $30 \times$ |  |  |  | + | + | + |
| $30 \times$ |  |  |  | + | + |  |
| $10 \times$ | + |  |  | + |  |  |
| $\cos t$ | 9 | 9 | 9 | 4 | 4 | 4 |

available budget: 30

| topic | \#votes | cost |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $t_{1}$ | 110 | 9 | $\bullet$ | $\bullet$ |
| $t_{2}$ | 100 | 9 | $\bullet$ |  |
| $t_{3}$ | 90 | 9 | $\bullet$ | $\bullet$ |
| $t_{4}$ | 70 | 4 |  | $\bullet$ |
| $t_{5}$ | 60 | 4 |  | $\bullet$ |
| $t_{6}$ | 30 |  |  | $\bullet$ |

Need to ensure fairness to groups of voters through proportionality

## 5. Complex alternatives $\rightarrow$ Judgment aggregation

We can select three topics. The votes of the attendees:

|  | $t_{1}$ | $t_{2}$ | $t_{3}$ | $t_{4}$ | $t_{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 5 voters | + | + | + |  |  |
| 3 voters | + | + |  |  | + |
| 1 voter |  |  |  | + | + |
| 1 voter |  |  | + |  | + |
| 2 voters |  |  |  | + |  |

Admissible committees are those that satisfy the constraint

$$
\left(t_{1} \vee t_{3}\right) \wedge\left(t_{2} \vee t_{5}\right) \wedge \neg\left(t_{1} \wedge t_{4} \wedge t_{5}\right) \wedge \neg\left(t_{2} \wedge t_{4} \wedge t_{5}\right) \wedge\left(t_{3} \rightarrow t_{4}\right)
$$

- focus on complex feasibility constraints


## 5. Complex alternatives

| focus on | proportionality <br> guarantees | complex <br> preferences | complex <br> constraints |
| :---: | :---: | :---: | :---: |
| combinatorial <br> domains |  | + |  |
| multiwinner <br> elections | + |  |  |
| participatory <br> budgeting | + |  | $(+)$ |
| judgment <br> aggregation |  |  | + |

Thanks: Dominik Peters

## 6. Diversity

- select 4 members for a committee
- ideal representation objectives
- 50\% male, $50 \%$ female
- $25 \%$ area $1,50 \%$ area $2,25 \%$ area 3.
- $25 \%$ junior, $75 \%$ senior.

|  | Gender | Area | Seniority |  |
| :---: | :---: | :---: | :---: | :---: |
| $c_{1}$ | $F$ | 1 | $J$ |  |
| $c_{2}$ | $M$ | 3 | $S$ |  |
| $c_{3}$ | $F$ | 1 | $S$ |  |
| $c_{4}$ | $M$ | 2 | $J$ |  |
| $c_{5}$ | $M$ | 2 | $J$ |  |
| $c_{6}$ | $M$ | 2 | $J$ |  |
| $c_{7}$ | $F$ | 2 | $J$ |  |
| $c_{8}$ | $M$ | 3 | $S$ |  |

## 6. Diversity

- select 4 members for a committee
- ideal representation objectives
- $50 \%$ male, $50 \%$ female
- $25 \%$ area $1,50 \%$ area $2,25 \%$ area 3.
- $25 \%$ junior, $75 \%$ senior.
$\times(50 / 50)$

|  | Gender | Area | Seniority |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| $c_{1}$ | $F$ | 1 | $J$ |
| $c_{2}$ | $M$ | 3 | $S$ |
| $c_{3}$ | $F$ | 1 | $S$ |
| $c_{4}$ | $M$ | 2 | $J$ |
| $c_{5}$ | $M$ | 2 | $J$ |
| $c_{6}$ | $M$ | 2 | $J$ |
| $c_{7}$ | $F$ | 2 | $J$ |
| $c_{8}$ | $M$ | 3 | $S$ |

## 6. Diversity

- select 4 members for a committee
- constraints:
- 50\% male, 50\% female
- 25\%-50 \% area 1, 40\%-60 \% area $2,10 \%-25 \%$ area 3.
- $\geq 25 \%$ junior, $\geq 50 \%$ senior.

|  | Gender | Area | Seniority |
| :---: | :---: | :---: | :---: |
| $c_{1}$ | $F$ | 1 | $J$ |
| $c_{2}$ | $M$ | 2 | $J$ |
| $c_{3}$ | $M$ | 2 | $S$ |
| $c_{4}$ | $F$ | 3 | $S$ |
| $c_{5}$ | $M$ | 2 | $J$ |
| $c_{6}$ | $M$ | 2 | $J$ |
| $c_{7}$ | $M$ | 2 | $J$ |
| $c_{8}$ | $F$ | 1 | $J$ |

Which committee should be elected?

## 6. Diversity

- select 4 members for a committee
- votes
- hard constraints:
- 50\% male, $50 \%$ female
- 25\%-50 \% area 1, 40\%-60 \% area 2, 10\%-25 \% area 3.
- $\geq 25 \%$ junior, $\geq 50 \%$ senior.

|  | Gender | Area | Seniority | $v_{1}$ | $v_{2}$ | $v_{3}$ | $v_{4}$ | $v_{5}$ | $v_{6}$ | $v_{7}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $c_{1}$ | $F$ | 1 | $J$ | + |  |  |  | + |  | + |
| $c_{2}$ | $M$ | 3 | $S$ | + |  |  |  |  |  | + |
| $c_{3}$ | $F$ | 1 | $S$ | + | + |  | + |  |  |  |
| $c_{4}$ | $M$ | 2 | $J$ |  |  |  | + |  |  |  |
| $c_{5}$ | $M$ | 2 | $J$ |  | + |  | + |  |  |  |
| $c_{6}$ | $M$ | 2 | $J$ |  |  |  |  |  | + | + |
| $c_{7}$ | $F$ | 2 | $J$ |  |  | + | + |  |  |  |
| $c_{8}$ | $M$ | 3 | $S$ |  |  | + |  | + |  |  |

Which committee should be elected?

## 6. Diversity: application to composing citizens' assemblies

- variant with randomized, fair selection
- variant with online selection


## 6. Diversity: application to composing citizens' assemblies

- variant with randomized, fair selection
- variant with online selection
- 50\% male, $50 \%$ female
- $25 \%$ area $1,50 \%$ area $2,25 \%$ area 3.
- 25\% junior, 75 \% senior.

| Gender | Area | Seniority | select? |
| :---: | :---: | :---: | :---: |
| $M$ | 3 | $J$ | yes |

## 6. Diversity: application to composing citizens' assemblies

- variant with randomized, fair selection
- variant with online selection
- 50\% male, $50 \%$ female
- $25 \%$ area $1,50 \%$ area $2,25 \%$ area 3.
- 25\% junior, 75 \% senior.

| Gender | Area | Seniority | select? |
| :---: | :---: | :---: | :---: |
| $M$ | 3 | $J$ | yes |
| $F$ | 3 | $J$ | no |

## 6. Diversity: application to composing citizens' assemblies

- variant with randomized, fair selection
- variant with online selection
- $50 \%$ male, $50 \%$ female
- $25 \%$ area $1,50 \%$ area $2,25 \%$ area 3.
- 25\% junior, 75 \% senior.

| Gender | Area | Seniority | select? |
| :---: | :---: | :---: | :---: |
| $M$ | 3 | $J$ | yes |
| $F$ | 3 | $J$ | no |
| $M$ | 1 | $S$ | yes |
| $\ldots$ | $\cdots$ | $\cdots$ | $\cdots$ |

- if the probability distribution on arrivals is known $\rightarrow$ Markov decision processes
- if not $\rightarrow$ reinforcement learning


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | $\mathbf{2}$ | $\mathbf{2}$ | 6 |
| Bob | 7 | $\mathbf{5}$ | 5 | 5 | 7 |
| Carol | $\mathbf{2 0}$ | 3 | 3 | 3 | 3 |

- $v_{\text {Bob }}(b)=5=$ value of item $b$ for Bob
- Assume agents have additive valuations:

$$
v_{B o b}(\{b, e\})=5+7=12
$$

- envy-freeness (EF): every agent $i$ weakly prefers her share to the share of any other agent $j$
- Ann prefers Bob's share $\{b, e\}$ to her own $\{c, d\}$ : the blue allocation is not envy-free
- There in no envy-free allocation!


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | $\mathbf{2}$ | $\mathbf{2}$ | 6 |
| Bob | 7 | $\mathbf{5}$ | 5 | 5 | $\mathbf{7}$ |
| Carol | $\mathbf{2 0}$ | 3 | 3 | 3 | 3 |

- A weakening of EF: envy-freeness up to one good (EF1):
- The blue allocation is EF1:
- Ann no longer envies Bob if we remove one good from Bob's share: $v_{A n n}(\{b, e\} \backslash\{e\})=3 \leq v_{\text {Ann }}(\{c, d\})=4$
- Ann no longer envies Carol if we remove one good from Carol's share: $v_{A n n}(\{a\} \backslash\{a\})=0 \leq v_{\text {Ann }}(\{c, d\})=4$
- Bob and Carol do not envy anyone.
- An EF1 allocation is guaranteed to exist (for additive valuations) and can be computed in polynomial time.


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | $\mathbf{2}$ | $\mathbf{2}$ | 6 |
| Bob | 7 | $\mathbf{5}$ | 5 | 5 | $\mathbf{7}$ |
| Carol | $\mathbf{2 0}$ | 3 | 3 | 3 | 3 |

- Between EF1 and EF: envy-freeness up to any good (EFX)
- Ann still envies Bob if we remove $b$ from Bob's share: $v_{\text {Ann }}(\{b, e\} \backslash\{b\})=6>v_{\text {Ann }}(\{c, d\})=4$
- the blue allocation is not EFX.


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | 2 | 2 | 6 |
| Bob | 7 | 5 | 5 | 5 | 7 |
| Carol | 20 | 3 | 3 | 3 | 3 |

- Between EF1 and EF: envy-freeness up to any good (EFX)
- the red allocation is EFX: removing any good from Bob's share eliminates Ann her envy towards Bob; and similarly for her envy to Carol.


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | 2 | 2 | 6 |
| Bob | 7 | 5 | 5 | 5 | 7 |
| Carol | 20 | 3 | 3 | 3 | 3 |

- Between EF1 and EF: envy-freeness up to any good (EFX)
- the red allocation is EFX
- does an EFX allocation always exist?


## 7. Fair Division of Indivisible Items

|  | $a$ | $b$ | $c$ | $d$ | $e$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ann | 15 | 3 | 2 | 2 | 6 |
| Bob | 7 | 5 | 5 | 5 | 7 |
| Carol | 20 | 3 | 3 | 3 | 3 |

- Between EF1 and EF: envy-freeness up to any good (EFX)
- the red allocation is EFX
- does an EFX allocation always exist? Long-standing open problem

| $\mathrm{EF} \longrightarrow \mathrm{EFX}$ | EF 1 |  |
| :---: | :--- | :--- |
| not guaranteed <br> for additive valuations |  | open problem |
| guaranteed |  |  |
| for additive valuations |  |  |

## 7. Fair Division of Indivisible Items



## 8. Automated Theorem Proving for Social Choice

- proving (or disproving) theorems in social choice is difficult because it involves large combinatorial structures
- SAT solvers can help!
- find new proofs for known results; discover new results; uncover mistakes in the literature

Example: two sided matching

- two groups of $n$ agents each
- each agent ranks the agents of the other group
- can we guarantee stability and fair treatment of both groups?
- no as soon as $n \geq 3$ !

Stability for $n=3$ : conjunction of 419,904 clauses


Thanks: Ulle Endriss

## 9. Collective decision making datasets

## Building \& maintaining

Dataset for voting data:
PrefLib.Org
Other datasets: matching, participatory budgeting
all open access

## Exploiting

Gap between theory and real-world instances?

Assessing the validity of preference models

Learning/ discovering structure
9. Collective decision making datasets

## Building \& maintaining

Dataset for voting data:
PrefLib.Org
Other datasets: matching, participatory budgeting
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## Exploiting

Gap between theory and real-world instances?

Assessing the validity of preference models

Learning/ discovering structure
"Map of real-world elections"
Source:
Boehmer, Bredereck, Faliszeswski, Niedermeier \& Szufa, 2021

Thanks: Piotr Faliszewski, Nick Mattei

## Social choice engineering at Université Paris-Dauphine



- huge construction works in the whole building 2022-2027
- one building, 600 offices, most occupied by one or two persons
- > $90 \%$ of the building will be completely rebuilt
- 5 big phases, whose duration is known with some uncertainty
- it is known which offices will be unavailable at each phase
- initial office allocation known, final state (almost) known
- people moving in average twice + possible compression at some intermediate phase

Students: this should not prevent you from coming and studying with uș!

## Social choice engineering at Université Paris-Dauphine

- the university asked us to help finding a fair and efficient reallocation sequence
- expertise needed in AI, OR and social choice
- a fair division problem? Yes but:
- 6 research labs + teaching departments + central services $\Longrightarrow$ not clear who the agents are: individuals, groups, both?
- heavily non-additive preferences: desire for labs/departments to remain grouped, for moves to be timewise not too close, ...
- uncertainty
temporal fair division problem with individual and group fairness, complex nonadditive preferences and uncertainty!
- each of these complications has been studied individually
- no known framework / algorithm for our problem
- social choice engineering! (here and elsewhere)


## Social Choice Engineering



What we know how to do
What is missing


## Summary: Social Choice and AI

new techniques new paradigms<br>new objects of study new applications

$$
\begin{array}{cc}
\text { multiagent systems } & \text { KR\&R } \\
\text { planning/MDP } & \text { online learning } \\
\text { statistical learning } & \text { SAT }
\end{array}
$$

user modelling?
NLP?

Special thanks: François Durand

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## Thanks to my frequent and/or recent coauthors

Pierre Marquis - Didier Dubois - Ulle Endriss - Yann Chevaleyre - Henri Prade - Lirong Xia - Sylvain Bouveret -
Andreas Herzig - Nicolas Maudet - Jérôme Monnot - Hélène Fargier - Haris Aziz - Vincent Conitzer -
Marija Slavkovik - Bruno Zanuttini - Elise Bonzon - Abdallah Saffidine - Marie-Christine Lagasquie Jérôme Mengin - Jörg Rothe - Leon van der Torre - Nathanaël Barrot - James Delgrande - Edith Elkind -
Julien Lesca - Manel Ayadi - Nahla Ben Amor - Hans van Ditmarsch - Florence Dupin de Saint-Cyr Piotr Faliszewski - Judy Goldsmith - Piotr Skowron - Nic Wilson - Mike Wooldridge - Dorothea Baumeister -
Andreas Darmann - Paul Harrenstein - Sarit Kraus - Srdjan Vesic - Peter Biró - Markus Brill - Iannis Caragiannis Laurent Gourvès - Ronald de Haan - Nick Mattei - Dominik Peters - Gabriella Pigozzi - Anja Rey Hilmar Schadrack - Lena Schend - Stéphane Airiau - Tahar Allouche - Jamal Atif - Felix Brandt Katarina Cechlarova - Théo Delemazure - Virginie Do - François Durand - Umberto Grandi - Hugo Gilbert Jatin Jindal - Justin Kruger - Anna Maria Kerkmann - Jean-François Laslier - Reshef Meir - Maria Polukarov -

François Schwarzentruber - Arkadii Slinko - Nicolas Usunier - Florian Yger - Bill Zwicker

## Vote on your preferred topics!



Informal paper and other resources coming with this talk:

https://www.lamsade.dauphine.fr/~lang/IJCAI22.html

